

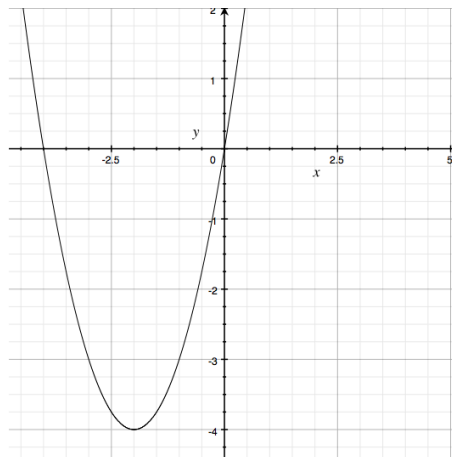
This exam is closed book. No graphing calculators or cell phones are allowed. No bathroom breaks are permitted while taking the exam. Good luck!

### 1 Multiple Choice (2 points each)

- (1) Find the limit if it exists:  $\lim_{x \rightarrow 2^+} \frac{\sqrt{x+2} - \sqrt{x}}{x-2}$   
(A) 0      (B)  $\frac{2-\sqrt{2}}{0}$       (C)  $\infty$       (D)  $-\infty$
- (2) Fill in the blanks: A derivative \_\_\_\_\_ the \_\_\_\_\_ change of a function for a given  $\Delta x$ .  
(A) equals, horizontal      (C) equals, vertical  
(B) approximates, horizontal      (D) approximates, vertical
- (3) Suppose that the value  $V$  of a machine depreciates with time  $t$  (measured in months) at the rate  $V(t) = 5 + e^{-0.15t+2}$ . Find  $\lim_{t \rightarrow \infty} V(t)$   
(A) 0      (B) 5      (C) 7      (D) 12
- (4) Find the average rate of change for  $f(x) = \sqrt{2x}$  if  $x$  increases from 2 to 18.  
(A)  $\frac{1}{4}$       (B)  $\frac{1}{3}$       (C)  $\frac{-3}{10}$       (D) 2
- (5) Find the instantaneous rate of change for  $f(x) = \sqrt{2x}$ , at  $x = 18$ .  
(A) 6      (B)  $\frac{1}{6}$       (C)  $\frac{1}{6\sqrt{2}}$       (D)  $\frac{1}{2\sqrt{2}}$
- (6) A firm faces the profit function  $P(x) = -3x^3 + 9x + 9$ . At what output level is profit maximized?  
(A)  $x = 0, \frac{4}{9}$       (B)  $x = 1, -1$       (C)  $x = \sqrt{3}$       (D)  $x = 1$
- (7) Suppose the firm in question (6) doubles production, from  $x = 1$  to  $x = 2$ . What is the marginal profit of producing the 2<sup>nd</sup> unit?  
(A) -\$12      (B) \$0      (C) -\$27      (D) \$3
- (8) Solve the matrix equation  $AX = B$  for  $X = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$ , where  $A = \begin{bmatrix} 5 & 6 \\ 4 & 5 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$   
(A)  $\begin{bmatrix} -7 \\ 6 \end{bmatrix}$       (B)  $\begin{bmatrix} 7 \\ -6 \end{bmatrix}$       (C)  $\begin{bmatrix} 5 & -6 \\ -4 & 5 \end{bmatrix}$       (D)  $\begin{bmatrix} 1 \\ 2 \end{bmatrix}$
- (9) Let  $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 6 & 1 & 3 \\ 47 & 7 & 1 \\ 1 & 8 & 2 \end{bmatrix}$ . Find the product  $AB$  if possible.  
(A)  $\begin{bmatrix} 6 & 1 & 3 \\ 47 & 7 & 1 \\ 1 & 8 & 2 \end{bmatrix}$       (B)  $\begin{bmatrix} 6 \\ 47 \\ 1 \end{bmatrix}$       (C)  $\begin{bmatrix} 6 & 0 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 2 \end{bmatrix}$       (D)  $[ 6 \ 1 \ 3 ]$

- (10) If  $f'(x) = 2x + 4$  and the graph of  $f(x)$  is given below, what is  $f(x)$ ?

- (A)  $f(x) = x^2 + 4x$   
 (B)  $f(x) = 2x^2 + 4x$   
 (C)  $f(x) = \frac{1}{2}x^2 + 4x$   
 (D)  $f(x) = (x - 2)^2 - 4$



## 2 Short Answer (3 points each)

**Remember:** number problems clearly, show all of your work, and circle your final answer.

- (11) Is the matrix  $N = \begin{bmatrix} -1 & -1 & 1 \\ -2 & -1 & 2 \\ -1 & -1/2 & 3/2 \end{bmatrix}$  the inverse of matrix  $M = \begin{bmatrix} 1 & -2 & 2 \\ -2 & 1 & 0 \\ 0 & -1 & 2 \end{bmatrix}$ ?

- (12) Labor and material costs for producing two guitar models are given:

<i>Model</i>	<i>Labor</i>	<i>Material</i>
A	\$30	\$20
B	\$40	\$30

In week 1, \$1,800 is allocated to labor and \$1,200 to materials. In week 2, \$1,750 and \$1,250 are. Use matrix equations to solve the quantities of each model,  $a$  and  $b$ , to produce each week.

- (13) A new firm lacks a functional model of their revenue. Fortunately, they've hired an analyst (you!) to help them *approximate* the change in their revenue from increasing production by from 55,700 to 56,300 units. Given that their marginal revenue when producing 55,700 units was \$18,000, what is their estimated change in revenue?
- (14) (i) Show that the *limit* of the difference quotient for  $f(x) = \frac{1}{x}$  is equal to its derivative,  $f'(x)$ , as found using derivative properties. (HINT:  $\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$  )
- (ii) Graph  $f(x)$ , evaluate  $f'(2)$ , then write the equation of the tangent line at  $x = 2$  and graph. (HINT:  $y - y_1 = m(x - x_1)$  )